

## Activity 38

## Operating with complex numbers

1. a)

number	Real part	Imaginary part
$u$	3	2
$v$	4	-4
$w$	-1	2

b)

(i)  $7 - 2i$

(ii)  $2 + 4i$

(iii) 6

(iv) It is the same as adding like terms

c)

(i)  $9 + 6i$

(ii)  $-7 + 14i$

(iii) Use rules for multiplying brackets, the real number times the complex number in brackets.

2. a)

(i)  $4I - 4I^2$

(ii)  $4 - 4i$

(iii)  $i^2 = -1$  and then collect like terms.

b)

(i)  $12 - 4I - 8I^2$

(ii)  $20 - 4i$

(iii)  $i^2 = -1$  and then collect like terms.

$4-4i \rightarrow v$	$3+2i$
$2i-1 \rightarrow w$	$4-4i$
$u+v$	$-1+2i$
$u+w$	$7-2i$
$u+v+w$	$2+4i$
$3u$	6
$7w$	$9+6i$
	$-7+14i$

Alg Standard Cplx Deg

3.

Expression	Number	Conjugate
$u$	$3 + 2i$	$3 - 2i$
$vi$	$4 + 4i$	$4 - 4i$
$uv$	$20 - 4i$	$20 + 4i$
$v^2$	$-32i$	$32i$
$(2i + 1)w$	$-5$	$-5$
$i^2$	$-1$	$-1$
$i^3$	$-i$	$i$
	$a + ib$	$a - ib$
$w\bar{w}$	$5$	$5$

$v \times i$	$4 + 4 \cdot i$
$u \times v$	$20 - 4 \cdot i$
$v^2$	$-32 \cdot i$
$(2i + 1)w$	$-5$
$i^2$	$-1$
$i^3$	$-i$
$w \times \text{conj}(w)$	$5$

4. When a complex number is multiplied by its conjugate the result is a **real** number.

5.

a) 
$$\frac{1}{5} - \frac{8i}{5} = \frac{1 - 8i}{5}$$

b) 
$$\frac{3 + 2i}{-1 + 2i} \times \frac{-1 - 2i}{-1 - 2i} = \frac{-3 - 6i - 2i - 4i^2}{1 - 4i^2} = \frac{-3 - 8i + 4}{1 + 4} = \frac{1 - 8i}{5}$$